

# sdcSpatial: Privacy protected density maps

Edwin de Jonge @edwindjonge

Statistics Netherlands Research & Development  
@edwindjonge

useR! 2019, July 11 2019

# sdcSpatial: Privacy protected maps



# sdcSpatial: Privacy protected maps

## Takeout message: sdcSpatial has methods for:

- **Creating** a raster map: `sdc_raster` for pop density, value density and mean density, using the excellent raster package by Hijmans (2019).
- **Finding out** which locations are **sensitive**: `plot_sensitive`, `is_sensitive`.
- Adjusting raster map for **protecting data**: `protect_smooth`, `protect_quadtree`.
- **Removing sensitive** locations.

# Who am I and why sdcSpatial?

- Statistical consultant, Data Scientist @cbs.nl / Statistics NL
- Statistics Netherlands is producer main official statistics in the Netherlands:
  - Stats on Demographics, economy (GDP), education, environment, agriculture, Finance etc.
  - Part of the European Statistical System, ESS.

## Motivation for sdcSpatial

- ESS has European Code of Statistical Practice (predates GDPR, European law on Data Protection):  
**no individual information may be revealed.**

# Sdc in sdcSpatial?

SDC = “Statistical Disclosure Control”

## Collection of statistical methods to:

- Check if data is safe to be published
- Protect data by slightly altering (aggregated) data
  - adding noise
  - shifting mass
- Most SDC methods operate on records.
- **sdcSpatial works upon locations.**

# Data

```
data(dwelling, package="sdcSpatial")  
nrow(dwelling)
```

```
## [1] 90603
```

```
head(dwelling) # consumption/unemployed are simulated!
```

```
##           x           y consumption unemployed  
## 1 149712 470104    2049.926      FALSE  
## 2 149639 469906    1814.938      FALSE  
## 3 149631 469888    2074.882      FALSE  
## 4 149788 469831    1927.989      FALSE  
## 5 149773 469834    2164.969      FALSE  
## 6 149688 469898    1987.958      FALSE
```

# Let's create a `sdc_raster`

## Creation:

```
library(sdcSpatial)
unemployed <- sdc_raster( dwellings[c("x", "y")] # realistic locations
                        , dwellings$unemployed # simulated data!
                        , r = 500 # raster resolution of 500m
                        , min_count = 10 # min support
                        )
```

## What has been created?

```
print(unemployed)

## logical sdc_raster object:
## resolution: 500 500 , max_risk: 0.95 , min_count: 10
## mean sensitivity score [0,1]: 0.4249471
```

42% of the data on this map is sensitive!

# What is sensitivity?

Binary score (logical) per raster cell indicating if it's unsafe to publish.

## Calculated:

- a) Per location  $(x_i, y_i)$  (raster cell)
- b) Using risk function `disclosure_risk`  $r(x, y) \in [0, 1]$ . How accurate can an attacker estimate the value of an individual?  
If  $r(x_i, y_i) > \text{max\_risk}$  then  $(x_i, y_i)$  is sensitive.
- c) Using a minimum number of observations.  
If  $\text{count}_i < \text{min\_count}$ , then  $(x_i, y_i)$  is sensitive.



# Disclosure risks

## External (numeric)

$$r(x, y) = \max \frac{v_i}{\sum_{i \in (x, y)} v_i} \text{ with } v_i \in \mathbb{R}$$

## Discrete (logical)

$$r(x, y) = \frac{1}{n} \sum_{i \in (x, y)} v_i \text{ with } v_i \in \{0, 1\}$$

# Type of raster density maps:

(Stored in `unemployed$value`):

Density can be area-based:

- **number of people** per square (`$count`): population density.
- **(total) value** per square (`$sum`): number of unemployed per square.

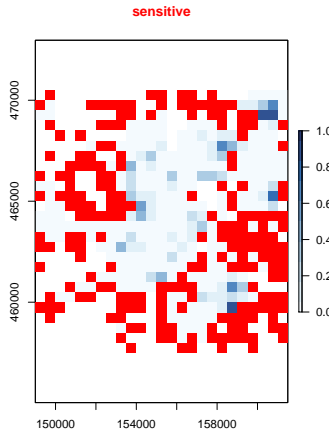
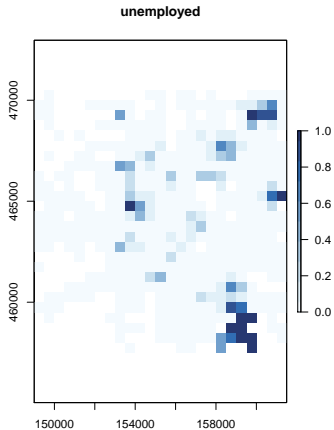
Or density can population-based:

- **Mean value** per square (`$mean`): unemployment rate per square.

*Note: All density types are valid, but (total) value per square strongly interacts with population density.  
(e.g. <https://xkcd.com/1138>).*

# Plotting a `sdc_raster`

```
plot(unemployed, "mean")
```



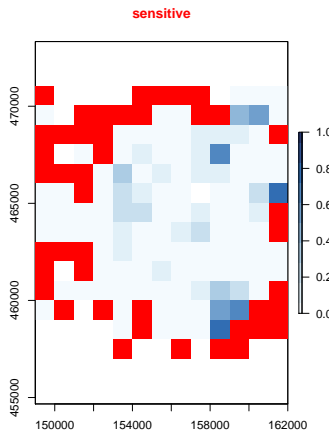
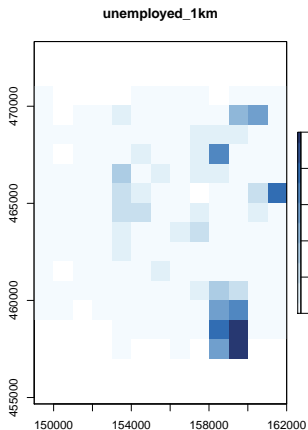
# How to reduce sensitivity?

## Options:

- a) Use a coarser raster: `sdcraster`.
- b) Apply spatial smoothing: `protect_smooth` method by Wolf and Jonge (2018), Jonge and Wolf (2016).
- c) Aggregate sensitive cells hierarchically with a quad tree until not sensitive: `protect_quadtree` method by Suñé et al. (2017).
- d) Remove sensitive locations: `remove_sensitive`.

# Option: coarser raster

```
unemployed_1km <- sdc_raster( dwellings[c("x", "y")]  
                             , dwellings$unemployed, r =1e3) # 1km!  
plot(unemployed_1km, "mean")
```



# Option: Coarsening

## Pros

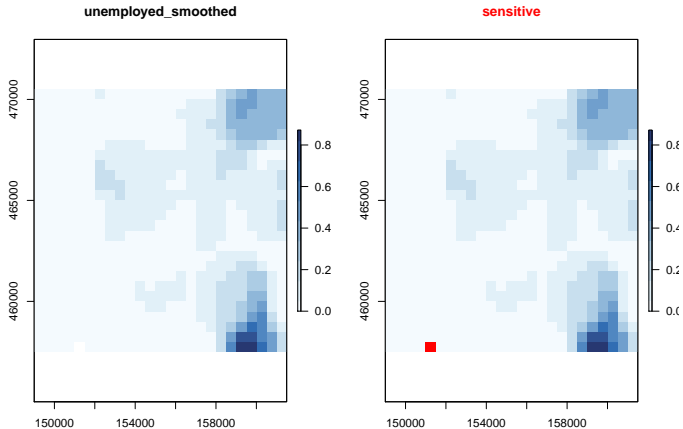
- Simple and easy explainable

## Cons

- Detailed spatial patterns are removed
- visually unattractive: “Blocky”

# Option: KDE-smoothing

```
unemployed_smoothed <- protect_smooth(unemployed, bw = 1500)  
plot(unemployed_smoothed, "mean")
```



# Options: KDE-smoothing

## Pro's

- Often enhances spatial pattern visualization, removing spatial noise.
- Makes it a density map and used as source for e.g. contour map.

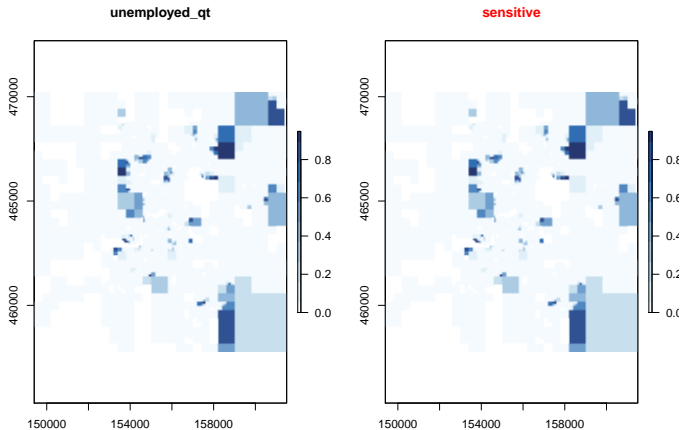
## Con's

- Does not remove all sensitive values (depends on bandwidth  $bw$ )
- A fixed band width is used for all locations: may remove detailed patterns. . .  
spatial processes often have location dependent band widths.  
(= future work)



# Option: Quad tree

```
unemployed_100m <- sdc_raster( dwellings[c("x","y")], dwellings$unemployed  
                             , r = 100) # use a finer raster  
unemployed_qt <- protect_quadtree(unemployed_100m)  
plot(unemployed_qt)
```



# Option: Quad tree

## Pro

- Adapts to data density
- Adjusts until no sensitive data is left.

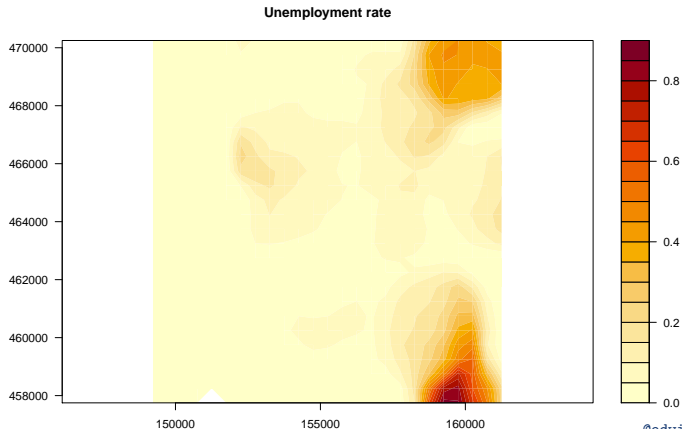
## Cons

- Visually: “Blocky” / “Mondrian-like” result.

# Publish: visual interpolation

So in 5 lines we create a visual attractive map that is safe:

```
unemployed <- sdc_raster(dwellings[c("x","y")], dwellings$unemployed, r=500)
unemployed_smoothed <- protect_smooth(unemployed, bw = 1500)
unemployed_safe <- remove_sensitive(unemployed_smoothed)
mean_unemployed <- mean(unemployed_safe)
raster::filledContour(mean_unemployed, main="Unemployment rate")
```



# The end

**Thank you for your attention!**

**Questions?**

**Curious?**

```
install.packages("sdcSpatial")
```

**Feedback and suggestions?**

<https://github.com/edwindj/sdcSpatial/issues>

# References

Hijmans, Robert J. 2019. *Raster: Geographic Data Analysis and Modeling*. <https://CRAN.R-project.org/package=raster>.

Jonge, Edwin de, and Peter-Paul de Wolf. 2016. “Spatial Smoothing and Statistical Disclosure Control.” In *Privacy in Statistical Databases*, edited by Josep Domingo-Ferrer and Mirjana Pejić-Bach, 107–17. Springer.

Suñé, E., C. Rovira, D. Ibáñez, and M. Farré. 2017. “Statistical Disclosure Control on Visualising Geocoded Population Data Using Quadrees.”  
[http://nt17.pg2.at/data/x\\_abstracts/x\\_abstract\\_286.docx](http://nt17.pg2.at/data/x_abstracts/x_abstract_286.docx).

Wolf, Peter-Paul de, and Edwin de Jonge. 2018. “Spatial Smoothing and Statistical Disclosure Control.” In *Privacy in Statistical Databases - Psd 2018*, edited by Josep Domingo-Ferrer and Francisco Montes Suay. Springer.